

Rules for Transformations of Graphs

Output	Transformation		Orientation/Type
$f(x)$	Original graph or parent graph.		
$f(x) + c$	Up c .		Vertical translation
$f(x) - c$	Down c .		Vertical translation
$f(x + c)$	Left c .		Horizontal translation
$f(x - c)$	Right c .		Horizontal translation
$-f(x)$	Reflects over the x -axis.		Vertical reflection
$f(-x)$	Reflects over the y -axis.		Horizontal reflection
$cf(x)$	If $c > 1$, then the graph is stretched.	* Vertical scaling, y changes, x does not change. Ex: If $c = 2$, then y is twice original.	Vertical stretch
	If $0 < c < 1$, then the graph is compressed.		Vertical compression
$f(cx)$	If $c > 1$, then the graph is compressed.	* Horizontal scaling, x changes, y does not change. Ex: if $c = 2$ then x is $\frac{1}{2}$ as much.	Horizontal compression
	If $0 < c < 1$, then the graph is stretched.		Horizontal stretch
$ f(x) $	Reflection of the <i>negative</i> y -values over the x -axis to become positive while all of the <i>positive</i> y 's stay the same.		Vertical
$f x $	Reflection of the <i>positive</i> x -values over the y -axis to replace the <i>negative</i> x -values creating a graph with y -axis symmetry.		Horizontal